

# Modeling the influence of acoustic loading on laryngeal self-sustained oscillations

Matías Zañartu, Luc Mongeau and George R. Wodicka

Ray W. Herrick Laboratories, Purdue University, West Lafayette, IN 47907

PURDUE  
UNIVERSITY  
Voice Production Laboratory

#2pSC4

## OBJECTIVE

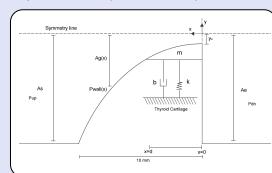
In this project, three-way interactions between sound waves in the subglottal and supraglottal tracts, the vibrations of the vocal folds, and laryngeal flow were investigated. The purpose was to determine if fluid-sound interactions were as significant as fluid-structure interactions during phonation. The effects of several acoustic loads on phonation were studied.

## INTRODUCTION

Different studies on voice production have demonstrated that forces that are in phase with the velocity of the tissue of the vocal folds are favorable to phonation (Rothenberg, 1981; Titze 1988; Fulcher et al., 2006). These forces can be produced by:  
 ✓ A 'mucosal wave' in the cover of the vocal folds. The driving force is produced by fluid-structure interactions.  
 ✓ An inertive impedance in the vocal tract ( $F_c < F_0$ ). The driving force is produced by fluid-sound interactions.  
 The relative importance between fluid-structure and fluid sound interaction in phonation is still unknown.  
 ✓ The role of other supraglottal loadings and the subglottal tract is not clear.  
 Traditional one-mass models cannot reach self-sustained oscillations (SSO) without acoustic loading, since the effects of the mucosal wave are not included.  
 ✓ For these models, the effects of the mucosal wave can be introduced in the flow instead of the structure using an orifice discharge coefficient (ODC).

## INTERACTIVE MODEL OF PHONATION

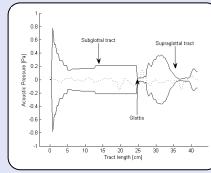
Based on a previous one-mass model (Fulcher et al., 2006), where negative Coulomb damping is used to drive the folds.  
 Fluid-structure interactions, fluid-sound interactions and collision effects were added to the previous model.  
 Bernoulli's equation and obstruction theory were used. A smooth time-varying ODC resembled the effects of the mucosal wave.  
 The ODC for converging and diverging glottal shapes were taken from experimental data (Park et al., 2006).



Half of the symmetric representation of the vocal folds model

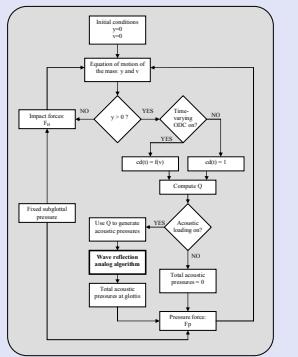
The acoustic loads were modeled using a wave reflection analog approach (Story, 1995; Rahim, 1994).

Contributions to this technique were made (see chart below).



Representation of the complete system -source and acoustic loads- using a wave reflection analog approach

- Material properties were taken from previous studies (Titze, 2002; Story and Titze, 1995).
- Equation of motion of the mass is given by:  
 $m\ddot{y} + b\dot{y} + k(y - y_s) = F_p$
- $F_p$  is the pressure force acting on the open cycle, including
  - ✓ Fluid-structure interactions
  - ✓ Fluid-sound interaction
- $F_M$  are the forces acting during collision, including
  - ✓ Hertz impact forces
  - ✓ Change in damping properties
  - ✓ Upstream pressure force on the non-colliding surface



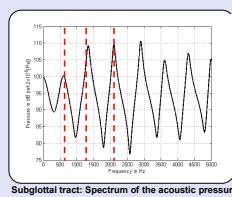
Values were comparable with other models for load scenarios (Story and Titze, 1995; Alipour et al., 2000).

## CONTRIBUTIONS TO THE WAVE ANALOG TECHNIQUE

New subglottal attenuation factor: global attenuation as by Rahim (1994). Subglottal tract losses were larger by roughly a factor of 3 compared with that of the vocal tract.

New subglottal tract design: Based on the area functions from Weibel (1963) with an adjusted termination. Results presented on the right.

- Complete set of tests to evaluate the scheme:
  - ✓ Comparison with theoretical complex solution
  - ✓ Effects of boundary conditions
  - ✓ Effects of radiation impedance
  - ✓ Effects of the global loss factor
  - ✓ Acoustic coupling between tracts



NOTE: The figure was constructed measuring the total response of the tract at the glottis.  $F_s=441$  KHz.

## COMPARISON BETWEEN INTERACTIONS

- Both fluid-structure interactions and fluid-sound interaction led to self-sustained oscillations
- Acoustic loading was more significant than the effects introduced by the orifice discharge coefficient.
- The influence of the subglottal tract appeared to be significant, but not as determinant as that of the vocal tract.

## EFFECTS OF THE ACOUSTIC LOADING

- Important changes were observed in the source (through the volumetric flow rate Q): Ripples and depressions that increased spectral components, changes in  $f_0$ .
- The less coupled with the loading, the more pronounced the effects were in the source.
- The supraglottal and subglottal tracts played different roles
- The inharmonicity was met only in the vocal tract
- The vocal tract was more dominant than the subglottal tract
- The subglottal tract reduced the effects introduced by the vocal tract in Q

## FLUID-STRUCTURE INTERACTIONS VS. FLUID-SOUND INTERACTIONS

### Research questions:

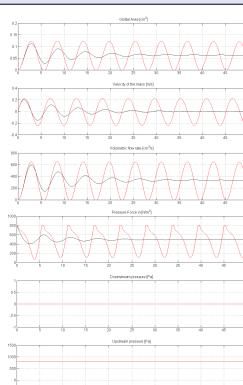
- What was the relative importance between fluid-structure interactions and fluid-sound interactions?
- What was the role of each tract?
- What were the effects of different acoustic loadings in SSO?

### Methods:

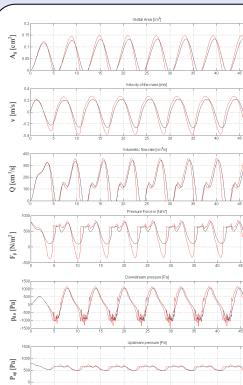
- Fluid-structure interactions were activated/deactivated through the time varying ODC.
- Three different cases were tested: No acoustic loading, subglottal tract + an inert supraglottal loading (vowel /i/), and subglottal tract + a less inert supraglottal loading (vowel /a/).

— : ODC OFF (no fluid-structure interactions)  
 - - : ODC ON (with fluid-structure interactions)

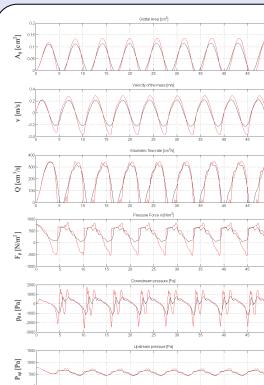
## NO ACOUSTIC LOADING



## MRI VOWEL /i/ + SUBGLOTTAL TRACT



## MRI VOWEL /a/ + SUBGLOTTAL TRACT



## Time history with no acoustic loading

- \*As = Ae = infinity
- \*Supraglottal formants:  $F_1 = n/a$ ,  $F_2 = n/a$
- \*Subglottal formants:  $F_1 = n/a$ ,  $F_2 = n/a$

- \*Fundamental frequency:  $f_0 = 180$  Hz
- \*The time-varying ODC yielded to SSO
- \*Without the time-varying ODC the vocal folds did not reach SSO
- \*The presence of acoustic loading was not a required condition to reach a steady state
- \*Collisions effects were not significant, for which the spectral analysis showed only a few harmonics

Values were comparable with other models for load scenarios (Story and Titze, 1995; Alipour et al., 2000).

## Time history with MRI vowel /i/ + subglottal tract

- \*As =  $2.7 \text{ cm}^2$ , Ae =  $0.33 \text{ cm}^2$
- \*Supraglottal formants:  $F_1 = 786$  Hz,  $F_2 = 2486$  Hz
- \*Subglottal formants:  $F_1 = 613$  Hz,  $F_2 = 1341$  Hz

- \*Fundamental frequency:  $f_0 = 170$  Hz
- \*Acoustic loading yielded to SSO
- \*Large coupling between source and vocal tract
- \*Subglottal tract: less pronounced effects in the source
- \*Modified source properties (Q): Reduced amplitude, added ripple on the opening phase and skewing.
- \*The presence of the time-varying ODC was not a required condition to reach a steady state
- \*When the time-varying ODC was introduced, larger variations were observed in Q,  $F_r$ , and  $P_{d,r}$
- \*The effect of collision were more significant.

## Time history with MRI vowel /a/ + subglottal tract

- \*As =  $2.7 \text{ cm}^2$ , Ae =  $0.45 \text{ cm}^2$
- \*Supraglottal formants:  $F_1 = 786$  Hz,  $F_2 = 1147$  Hz
- \*Subglottal formant:  $F_1 = 613$  Hz,  $F_2 = 1341$  Hz

- \*Fundamental frequency:  $f_0 = 90$  Hz
- \*Acoustic loading yielded to SSO
- \*Larger coupling between source and vocal tract
- \*Subglottal tract: did not vary significantly
- \*Modified source properties (Q): Reduced amplitude, added ripple on the opening phase and skewing.
- \*The presence of the time-varying ODC was not a required condition to reach a steady state
- \*When the time-varying ODC was introduced, larger variations were observed in Q,  $F_r$ , and  $P_{d,r}$
- \*The effect of collision were more significant.

## CONCLUSIONS

### COMPARISON BETWEEN INTERACTIONS

- Both fluid-structure interactions and fluid-sound interaction led to self-sustained oscillations
- Acoustic loading was more significant than the effects introduced by the orifice discharge coefficient.
- The influence of the subglottal tract appeared to be significant, but not as determinant as that of the vocal tract.

### GENERAL

- The interactive one-mass model was able to illustrate the same effects often seen in high order models.
- Results comparable with other studies using finite elements (Alipour et al., 2000) and higher order models (Story and Titze, 1995).

## FUTURE WORK

- Improve subglottal tract design: enhance the current wave reflection analog design.
- Improvements in the source model: pressure distribution codebook, or interactive high order model (finite element model).
- Theoretical perspective: develop a complete impedance analysis and an interactive state model.
- Experimental perspective: use synthetic models of the vocal folds using the acoustic loadings. Digital image correlation is suggested.

## REFERENCES

- Zañartu, M. (2008). "Influence of Acoustic Loading on the Flow-Induced Oscillations of Single Mass Models of the Human Larynx". M.S. Thesis, School of Electrical and Computer Engineering, Purdue University.
- Fulcher, J. P., G. M. Rahim, R. C. Melnyk, A. and Galvao, V. (2006). "Negative Coulomb damping, limiting cycles, and self-oscillation of the vocal folds". *J. Acoust. Soc. Am.*, **119**(4), pp. 386-395.
- Park, J. B. and Mongeau, L. (2006). "Instantaneous orifice discharge coefficients as measurements of glottal closure in the vocal folds". *J. Acoust. Soc. Am.*, **119**(4), pp. 396-405.
- Alipour, F., Berry, D. A. and Tait, I. R. (2000). "A finite element model of vocal fold vibration". *J. Acoust. Soc. Am.*, **107**(4), pp. 1850-1859.
- Harper, V. P. (2000). "Respiratory Tract Acoustical Modeling and Measurements". Ph.D. Dissertation., School of Electrical and Computer Engineering, Purdue University, 2000.
- Story, B. H. (1995). "A wave reflection analog approach to the vocal folds". *J. Acoust. Soc. Am.*, **97**(4), pp. 1337-1354.
- Story, B. H. (1998). "Vocal fold self-oscillation with a body-cover model of the vocal folds". *J. Acoust. Soc. Am.*, **97**(2), pp. 1249-1259.
- Story, B. H. (1999). "Physiologically-Based Speech Synthesis Using an Enhanced Reference Model of the Vocal Folds". Ph.D. Dissertation, University of New Mexico.
- Rahim, M. G. (1994). "Artificial Neural Networks for Speech Analysis/Synthesis", First edition, Kluwer Academic Publishers, New York.
- Titze, I. R. (1988). "The quasi-periodic amplitude oscillation of the vocal folds". *J. Acoust. Soc. Am.*, **83**, pp. 1538-1552.
- Titze, I. R. (1992). "Predicting glottal airflow in phonation: Application of the maximum power transfer theorem to a low-dimensional phonological model". *J. Acoust. Soc. Am.*, **91**(1), pp. 367-376.
- Rothenberg, M. (1981). "Acoustic interaction between the glottal source and the vocal tract". In: *Vocal Fold Physiology*. K. N. Stevens and M. Hirata Eds., University of Tokyo Press, Tokyo.
- Weibel, E. R. (1963). "Morphometry of the Human Lung", First Edition, New York, Springer.

## ACKNOWLEDGMENTS

- This project was funded by the National Institute on Deafness and Other Communication Disorders NICHD, National Institutes of Health (NIH), grant number R01 DC05798, the Fubright Program, the Institute of International Education and Purdue University.

- Fulcher, J. P., G. M. Rahim, R. C. Melnyk, A. and Galvao, V. (2006). "Negative Coulomb damping, limiting cycles, and self-oscillation of the vocal folds". *J. Acoust. Soc. Am.*, **119**(4), pp. 386-395.

- Story, B. H. (1998). "Vocal fold self-oscillation with a body-cover model of the vocal folds". *J. Acoust. Soc. Am.*, **97**(2), pp. 1249-1259.

- Story, B. H. (1999). "Physiologically-Based Speech Synthesis Using an Enhanced Reference Model of the Vocal Folds". Ph.D. Dissertation, University of New Mexico.

- Titze, I. R. (1988). "The quasi-periodic amplitude oscillation of the vocal folds". *J. Acoust. Soc. Am.*, **83**, pp. 1538-1552.

- Titze, I. R. (1992). "Predicting glottal airflow in phonation: Application of the maximum power transfer theorem to a low-dimensional phonological model". *J. Acoust. Soc. Am.*, **91**(1), pp. 367-376.

- Rothenberg, M. (1981). "Acoustic interaction between the glottal source and the vocal tract". In: *Vocal Fold Physiology*. K. N. Stevens and M. Hirata Eds., University of Tokyo Press, Tokyo.

- Weibel, E. R. (1963). "Morphometry of the Human Lung", First Edition, New York, Springer.

- Galvao, V. (2006). "Negative Coulomb damping, limiting cycles, and self-oscillation of the vocal folds". *J. Acoust. Soc. Am.*, **119**(4), pp. 386-395.

- Story, B. H. (1998). "Vocal fold self-oscillation with a body-cover model of the vocal folds". *J. Acoust. Soc. Am.*, **97**(2), pp. 1249-1259.

- Story, B. H. (1999). "Physiologically-Based Speech Synthesis Using an Enhanced Reference Model of the Vocal Folds". Ph.D. Dissertation, University of New Mexico.

- Titze, I. R. (1988). "The quasi-periodic amplitude oscillation of the vocal folds". *J. Acoust. Soc. Am.*, **83**, pp. 1538-1552.

- Titze, I. R. (1992). "Predicting glottal airflow in phonation: Application of the maximum power transfer theorem to a low-dimensional phonological model". *J. Acoust. Soc. Am.*, **91**(1), pp. 367-376.

- Rothenberg, M. (1981). "Acoustic interaction between the glottal source and the vocal tract". In: *Vocal Fold Physiology*. K. N. Stevens and M. Hirata Eds., University of Tokyo Press, Tokyo.

- Weibel, E. R. (1963). "Morphometry of the Human Lung", First Edition, New York, Springer.

- Galvao, V. (2006). "Negative Coulomb damping, limiting cycles, and self-oscillation of the vocal folds". *J. Acoust. Soc. Am.*, **119**(4), pp. 386-395.

- Story, B. H. (1998). "Vocal fold self-oscillation with a body-cover model of the vocal folds". *J. Acoust. Soc. Am.*, **97**(2), pp. 1249-1259.

- Story, B. H. (1999). "Physiologically-Based Speech Synthesis Using an Enhanced Reference Model of the Vocal Folds". Ph.D. Dissertation, University of New Mexico.

- Titze, I. R. (1988). "The quasi-periodic amplitude oscillation of the vocal folds". *J. Acoust. Soc. Am.*, **83**, pp. 1538-1552.

- Titze, I. R. (1992). "Predicting glottal airflow in phonation: Application of the maximum power transfer theorem to a low-dimensional phonological model". *J. Acoust. Soc. Am.*, **91**(1), pp. 367-376.

- Rothenberg, M. (1981). "Acoustic interaction between the glottal source and the vocal tract". In: *Vocal Fold Physiology*. K. N. Stevens and M. Hirata Eds., University of Tokyo Press, Tokyo.

- Weibel, E. R. (1963). "Morphometry of the Human Lung", First Edition, New York, Springer.

- Galvao, V. (2006). "Negative Coulomb damping, limiting cycles, and self-oscillation of the vocal folds". *J. Acoust. Soc. Am.*, **119**(4), pp. 386-395.

- Story, B. H. (1998). "Vocal fold self-oscillation with a body-cover model of the vocal folds". *J. Acoust. Soc. Am.*, **97**(2), pp. 1249-1259.

- Story, B. H. (1999). "Physiologically-Based Speech Synthesis Using an Enhanced Reference Model of the Vocal Folds". Ph.D. Dissertation, University of New Mexico.

- Titze, I. R. (1988). "The quasi-periodic amplitude oscillation of the vocal folds". *J. Acoust. Soc. Am.*, **83**, pp. 1538-1552.

- Titze, I. R. (1992). "Predicting glottal airflow in phonation: Application of the maximum power transfer theorem to a low-dimensional phonological model". *J. Acoust. Soc. Am.*, **91**(1), pp. 367-376.

- Rothenberg, M. (1981). "Acoustic interaction between the glottal source and the vocal tract". In: *Vocal Fold Physiology*. K. N. Stevens and M. Hirata Eds., University of Tokyo Press, Tokyo.

- Weibel, E. R. (1963). "Morphometry of the Human Lung", First Edition, New York, Springer.

- Galvao, V. (2006). "Negative Coulomb damping, limiting cycles, and self-oscillation of the vocal folds". *J. Acoust. Soc. Am.*, **119**(4), pp. 386-395.

- Story, B. H. (1998). "Vocal fold self-oscillation with a body-cover model of the vocal folds". *J. Acoust. Soc. Am.*, **97**(2), pp. 1249-1259.

- Story, B. H. (1999). "Physiologically-Based Speech Synthesis Using an Enhanced Reference Model of the Vocal Folds". Ph.D. Dissertation, University of New Mexico.

- Titze, I. R. (1988). "The quasi-periodic amplitude oscillation of the vocal folds". *J. Acoust. Soc. Am.*, **83**, pp. 1538-1552.

- Titze, I. R. (1992). "Predicting glottal airflow in phonation: Application of the maximum power transfer theorem to a low-dimensional phonological model". *J. Acoust. Soc. Am.*, **91**(1), pp. 367-376.

- Rothenberg, M. (1981). "Acoustic interaction between the glottal source and the vocal tract". In: *Vocal Fold Physiology*. K. N. Stevens and M. Hirata Eds., University of Tokyo Press, Tokyo.

- Weibel, E. R. (1963). "Morphometry of the Human Lung", First Edition, New York, Springer.

- Galvao, V. (2006). "Negative Coulomb damping, limiting cycles, and self-oscillation of the vocal folds". *J. Acoust. Soc. Am.*, **119**(4), pp. 386-395.

- Story, B. H. (1998). "Vocal fold self-oscillation with a body-cover model of the vocal folds". *J. Acoust. Soc. Am.*, **97**(2), pp. 1249-1259.

- Story, B. H. (1999). "Physiologically-Based Speech Synthesis Using an Enhanced Reference Model of the Vocal Folds". Ph.D. Dissertation, University of New Mexico.

- Titze, I. R. (1988). "The quasi-periodic amplitude oscillation of the vocal folds". *J. Acoust. Soc. Am.*, **83**, pp. 1538-1552.

- Titze, I. R. (1992). "Predicting glottal airflow in phonation: Application of the maximum power transfer theorem to a low-dimensional phonological model". *J. Acoust. Soc. Am.*, **91**(1), pp. 367-376.

- Rothenberg, M. (1981). "Acoustic interaction between the glottal source and the vocal tract". In: *Vocal Fold Physiology*. K. N. Stevens and M. Hirata Eds., University of Tokyo Press, Tokyo.

- Weibel, E. R. (1963). "Morphometry of the Human Lung", First Edition, New York, Springer.

- Galvao, V. (2006). "Negative Coulomb damping, limiting cycles, and self-oscillation of the vocal folds". *J. Acoust. Soc. Am.*, **119**(4), pp. 386-395.

- Story, B. H. (1998). "Vocal fold self-oscillation with a body-cover model of the vocal folds". *J. Acoust. Soc. Am.*, **97**(2), pp. 1249-1259.

- Story, B. H. (1999). "Physiologically-Based Speech Synthesis Using an Enhanced Reference Model of the Vocal Folds". Ph.D. Dissertation, University of New Mexico.

- Titze, I. R. (1988). "The quasi-periodic amplitude oscillation of the vocal folds". *J. Acoust. Soc. Am.*, **83**, pp. 1538-1552.

- Titze, I. R. (1992). "Predicting glottal airflow in phonation: Application of the maximum power transfer theorem to a low-dimensional phonological model". *J. Acoust. Soc. Am.*, **91**(1), pp. 367-376.

- Rothenberg, M. (1981). "Acoustic interaction between the glottal source and the vocal tract". In: *Vocal Fold Physiology*. K. N. Stevens and M. Hirata Eds., University of Tokyo Press, Tokyo.

- Weibel, E. R. (1963). "Morphometry of the Human Lung", First Edition, New York, Springer.

- Galvao, V. (2006). "Negative Coulomb damping, limiting cycles, and self-oscillation of the vocal folds". *J. Acoust. Soc. Am.*, **119**(4), pp. 386-395.

- Story, B. H. (1998). "Vocal fold self-oscillation with a body-cover model of the vocal folds". *J. Acoust. Soc. Am.*, **97**(2), pp. 1249-1259.

- Story, B. H. (1999). "Physiologically-Based Speech Synthesis Using an Enhanced Reference Model of the Vocal Folds". Ph.D. Dissertation, University of New Mexico.

- Titze, I. R. (1988). "The quasi-periodic amplitude oscillation of the vocal folds". *J. Acoust. Soc. Am.*, **83**, pp. 1538-1552.

- Titze, I. R. (1992). "Predicting glottal airflow in phonation: Application of the maximum power transfer theorem to a low-dimensional phonological model". *J. Acoust. Soc. Am.*, **91**(1), pp. 367-376.

- Rothenberg, M. (1981). "Acoustic interaction between the glottal source and the vocal tract". In: *Vocal Fold Physiology*. K. N. Stevens and M. Hirata Eds., University of Tokyo Press, Tokyo.

- Weibel, E. R. (1963). "Morphometry of the Human Lung", First Edition, New York, Springer.

- Galvao, V. (2006). "Negative Coulomb damping, limiting cycles, and self-oscillation of the vocal folds". *J. Acoust. Soc. Am.*, **119**(4), pp. 386-395.

- Story, B. H. (1998). "Vocal fold self-oscillation with a body-cover model of the vocal folds